

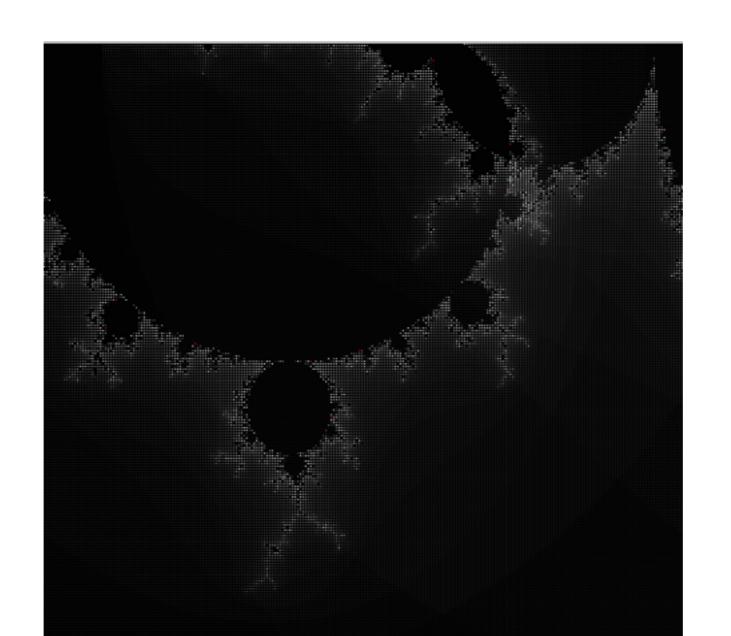
pure python code

Main took 0:00:12.465387 Main took 0:00:01.190245

python pure_python.py 1000 1000 pypy pure_python.py 1000 1000

pure python code Main took 0:00:08.769609 better referencing Main took 0:00:00.863155

python pure_python_2.py 1000 1000 pypy pure_python_2.py 1000 1000



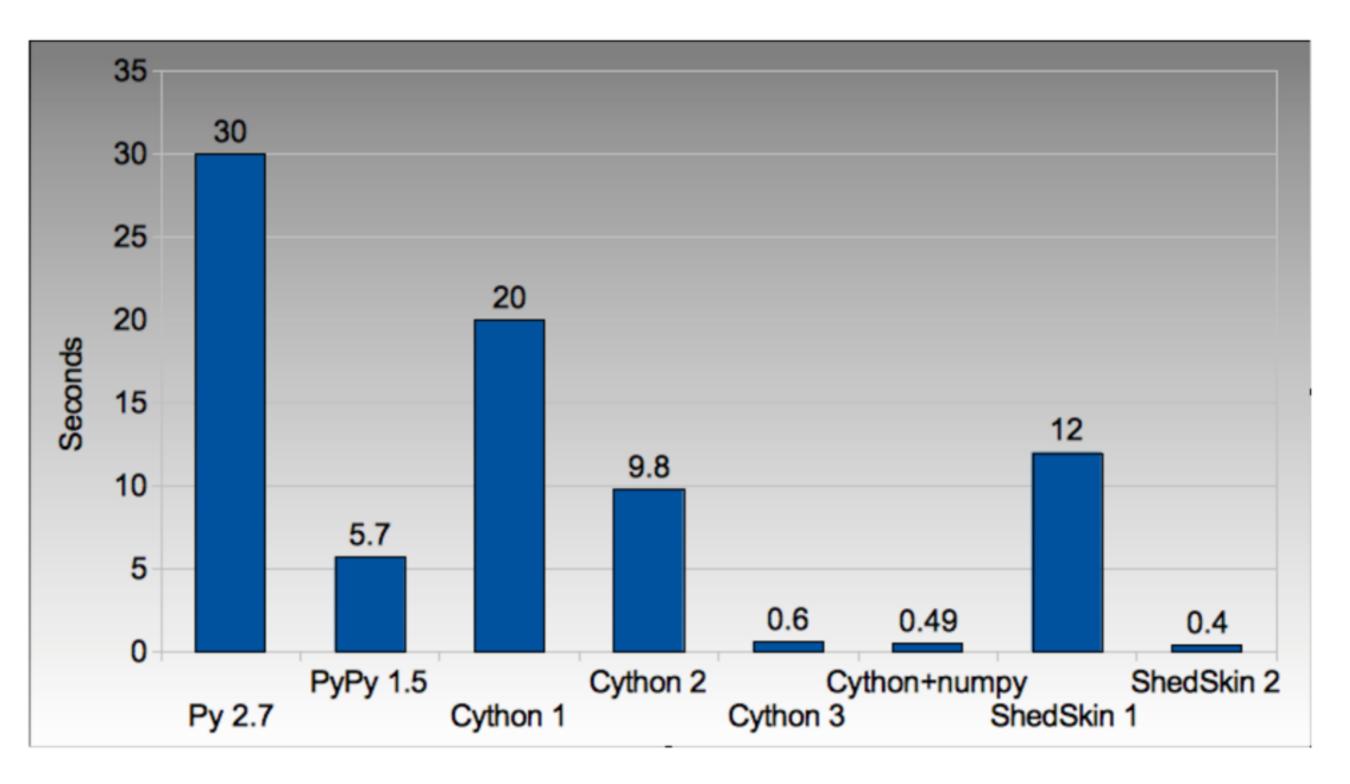


Figure 4.1: Run times on laptop for Python/C implementations

The profile module is the standard way to profile Python code, take a look at it here http://docs.python.org/library/profile.html. We'll run it on our simple Python implementation:

python -m cProfile -o rep.prof pure_python.py 1000 1000

This generates a rep.prof output file containing the profiling results, we can now load this into the pstats module and print out the top 10 slowest functions:

```
import pstats
p = pstats.Stats('rep.prof')
p.sort_stats('cumulative').print_stats(10)
```

```
p.sort stats('cumulative').print stats(10)
                           rep.prof
Thu Feb 19 08:11:49 2015
         51927850 function calls (51927727 primitive calls) in 18.920 seconds
  Ordered by: cumulative time
  List reduced from 656 to 10 due to restriction <10>
  ncalls tottime percall cumtime percall filename: lineno(function)
            0.011
                     0.011
                             18.920
                                      18.920 pure python.py:1(<module>)
        1
        1
            0.077
                    0.077
                             18.909
                                      18.909 pure python.py:23(calc pure python)
           14.250
                    14.250
                             18.610
                                      18.610 pure python.py:9(calculate z serial purepython)
        1
 51414419
          3.366
                    0.000
                              3.366
                                       0.000 {abs}
  250076
          0.994
                     0.000
                              0.994
                                       0.000 {range}
            0.008
                     0.008
                              0.154
                                       0.154 /usr/local/lib/python2.7/site-packages/numpy/ init .py:106(<mo
        1
        1
            0.000
                     0.000
                              0.118
                                       0.118 /usr/local/lib/python2.7/site-packages/numpy/add newdocs.py:10(<
                                       0.116 /usr/local/lib/python2.7/site-packages/numpy/lib/ init .py:1(<
        1
            0.009
                     0.009
                              0.116
                                       0.092 /usr/local/lib/python2.7/site-packages/numpy/lib/type check.py:3
        1
            0.001
                     0.001
                              0.092
        1
            0.017
                     0.017
                              0.091
                                       0.091 /usr/local/lib/python2.7/site-packages/numpy/core/ init .py:10
```

<pstats.Stats instance at 0x110a2b518>

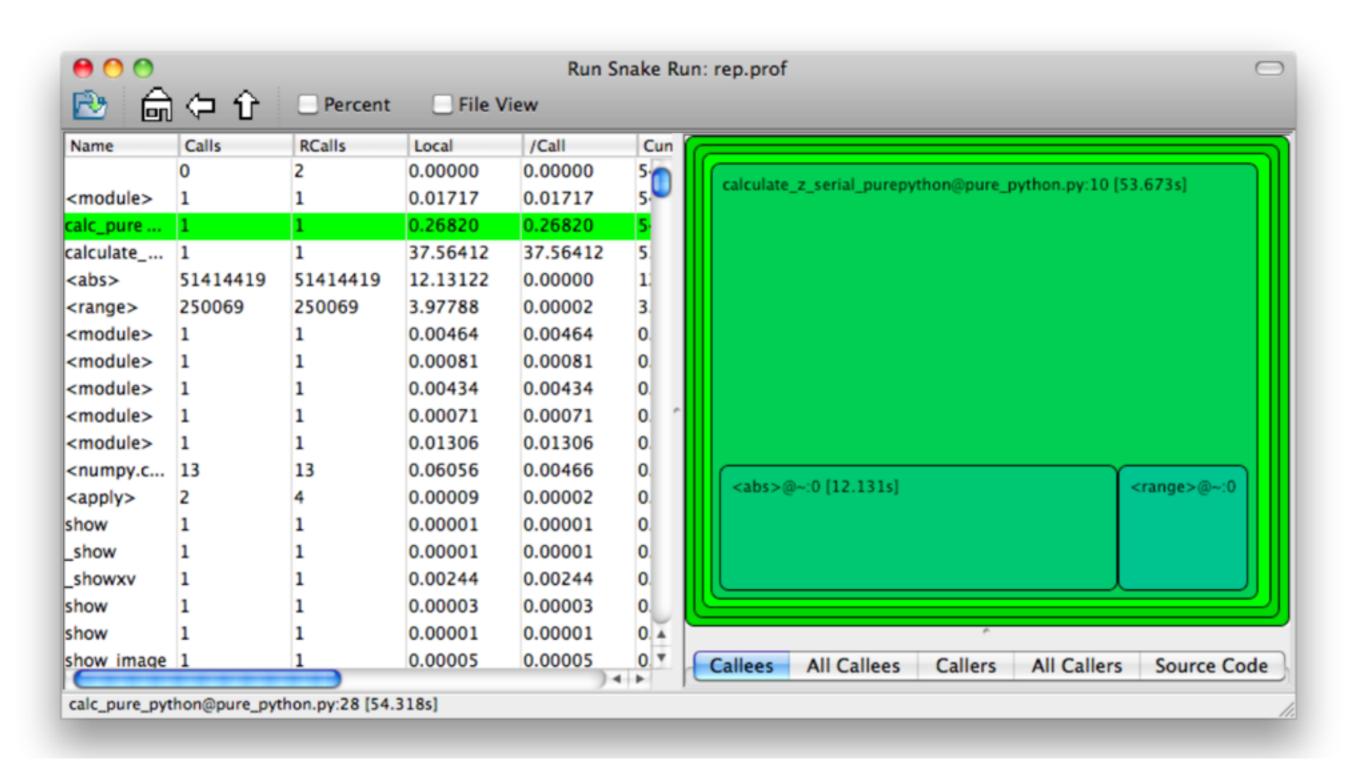
import pstats

p = pstats.Stats('rep.prof')

For more complex programs the output becomes hard to understand. runsnake is a great tool to visualise the profiled results:

>> runsnake rep.prof

This generates a display like:



However - which lines are causing our code to run slow? This is the more interesting question and cProfile can't answer it.

Let's look at the line_profer module. First we have to decorate our chosen function with @profile:

```
@profile
def calculate_z_serial_purepython(q, maxiter, z):
```

Next we'll run kernprof.py and ask it to do line-by-line profiling and to give us a visual output, then we tell it what to profile. **Note** that we're running a much smaller problem as line-by-line profiling takes ages:

```
>> kernprof.py -l -v pure_python.py 300 100
```

pip install line_profiler

Total sum of elements (for validation): 75014 Wrote profile results to pure_python.py.lprof

Timer unit: 1e-06 s

Total time: 0.806372 s File: pure_python.py

Function: calculate_z_serial_purepython at line 9

Line #	Hits	Time	Per Hit	% Time	Line Contents
9			=======	=======	@profile
10					def calculate_z_serial_purepython(q, maxiter,
11					"""Pure python with complex datatype, ite
12	1	128	128.0	0.0	output = [0] * len(q)
13	22501	9281	0.4	1.2	for i in range(len(q)):
14	22500	9853	0.4	1.2	if i % 1000 == 0:
15					<pre># print out some progress info si</pre>
16	23	403	17.5	0.0	print "%0.2f%% complete" % (1.0/l
17	560314	220829	0.4	27.4	<pre>for iteration in range(maxiter):</pre>
18	555686	293387	0.5	36.4	z[i] = z[i]*z[i] + q[i]
19	555686	255247	0.5	31.7	if abs($z[i]$) > 2.0:
20	17872	7377	0.4	0.9	<pre>output[i] = iteration</pre>
21	17872	9866	0.6	1.2	break
22	1	1	1.0	0.0	return output

```
18
19
```

z[i] = z[i]*z[i] + q[i] if abs(z[i]) > 2.0:

```
>>> import pure_python # imports our solver into Python
>>> dis.dis(pure_python.calculate_z_serial_purepython)
. . . .
18
                                       2 (z) # load z
           109 LOAD_FAST
           112 LOAD_FAST
                                       4 (i) # load i
           115 BINARY_SUBSCR
                                               # get value in z[i]
                                       2 (z) # load z
           116 LOAD_FAST
           119 LOAD_FAST
                                       4 (i) # load i
           122 BINARY_SUBSCR
                                               # get value in z[i]
           123 BINARY_MULTIPLY
                                               # z[i] * z[i]
                                       0 (q) # load z
           124 LOAD_FAST
           127 LOAD_FAST
                                       4 (i) # load i
           130 BINARY SUBSCR
                                               # get g[i]
                                               # add q[i] to last multiply
           131 BINARY_ADD
                                       2 (z) # load z
           132 LOAD_FAST
           135 LOAD FAST
                                       4 (i) # load i
           138 STORE_SUBSCR
                                               # store result in z[i]
19
           139 LOAD_GLOBAL
                                       2 (abs) # load abs function
           142 LOAD_FAST
                                       2 (z) # load z
           145 LOAD_FAST
                                       4 (i) # load i
           148 BINARY_SUBSCR
                                               # get z[i]
                                       1 # call abs
           149 CALL FUNCTION
           152 LOAD_CONST
                                      6 (2.0) # load 2.0
                                      4 (>) # compare result of abs with 2.0
           155 COMPARE_OP
           158 POP_JUMP_IF_FALSE
                                               # jump depending on result
                                     103
```

. . .

```
def calculate_z_serial_purepython(q, maxiter, z):
def calculate_z_serial_purepython(q, maxiter, z):
                                                                                                                      """Pure python with complex datatype, iterating over list of q and z"""
   """Pure python with complex datatype, iterating over list of q and z"""
                                                                                                                      output = [0] * len(q)
   output = [0] * len(q)
                                                                                                                      for i in range(len(q)):
    for i in range(len(q)):
                                                                                                                          zi = z[i]
        if i % 1000 == 0:
                                                                                                                          qi = q[i]
           # print out some progress info since it is so slow...
                                                                                                                          if i % 1000 == 0:
            print "%0.2f% complete" % (1.0/len(q) * i * 100)
                                                                                                                              # print out some progress info since it is so slow...
        for iteration in range(maxiter):
                                                                                                                              print "%0.2f%% complete" % (1.0/len(q) * i * 100)
            z[i] = z[i]*z[i] + q[i]
                                                                                                                          for iteration in range(maxiter):
            if abs(z[i]) > 2.0:
                                                                                                                              \#z[i] = z[i]*z[i] + q[i]
                output[i] = iteration
                                                                                                                              zi = zi * zi + qi
                                                                                                                              #if abs(z[i]) > 2.0
   return output
                                                                                                                              if abs(zi) > 2.0:
                                                                                                                                  output[i] = iteration
                                                                                                                      return output
```

def calculate z serial purepython(q, maxiter, z):

return output

pure python code

pure python code

improved

```
output = [0] * len(q)
   for i in range(len(q)):
       if i % 1000 == 0:
           # print out some progress info since it is so slow...
           print "%0.2f% complete" % (1.0/len(q) * i * 100)
       for iteration in range(maxiter):
           z[i] = z[i]*z[i] + q[i]
           if abs(z[i]) > 2.0:
               output[i] = iteration
               break
   return output
def calculate_z_serial_purepython(q, maxiter, z):
    """Pure python with complex datatype, iterating over list of g and z"""
   output = [0] * len(q)
    for i in range(len(q)):
        zi = z[i]
        qi = q[i]
        if i % 1000 == 0:
            # print out some progress info since it is so slow...
            print "%0.2f% complete" % (1.0/len(q) * i * 100)
        for iteration in range(maxiter):
            \#z[i] = z[i]*z[i] + q[i]
            zi = zi * zi + qi
            #if abs(z[i]) > 2.0:
            if abs(zi) > 2.0:
                output[i] = iteration
                break
```

"""Pure python with complex datatype, iterating over list of q and z"""

Total time: 0.804272 s

File: pure_python_2.py
Function: calculate_z_serial_purepython at line 10

Line #	Hits	Time	Per Hit	% Time	Line Contents
10 11 12					<pre>def calculate_z_serial_purepython(q, maxit """Pure python with complex datatype, i</pre>
13	1	119	119.0	0.0	output = $[0] * len(q)$
14	22501	9386	0.4	1.2	for i in range(len(q)):
15	22500	9574	0.4	1.2	zi = z[i]
16	22500	9512	0.4	1.2	qi = q[i]
17	22500	10169	0.5	1.3	if i % 1000 == 0:
18					<pre># print out some progress info</pre>
19	23	437	19.0	0.1	print "%0.2f%% complete" % (1.0/
20	560314	231067	0.4	28.7	for iteration in range(maxiter):
21					#z[i] = z[i]*z[i] + q[i]
22	555686	257318	0.5	32.0	zi = zi * zi + qi
23					#if abs(z[i]) > 2.0:
24	555686	258388	0.5	32.1	if abs(zi) > 2.0:
25	17872	7872	0.4	1.0	<pre>output[i] = iteration</pre>
26	17872	10429	0.6	1.3	break
27	1	1	1.0	0.0	return output

```
for iteration in range(maxiter)
            z[i] = z[i] * z[i] + q[i]
21
22
            zi = zi * zi + qi
            #if abs(z[i]) > 2.0:
23
24
            if abs(zi) > 2.0:
25
               output[i] = iteration
               break
         >> 123 FOR ITER
                                               52 (to 178)
                                                 7 (iteration)
              126 STORE FAST
 22
                                                5 (zi)
              129 LOAD FAST
              132 LOAD_FAST
                                                 5 (zi)
              135 BINARY MULTIPLY
              136 LOAD FAST
                                                 6 (qi)
              139 BINARY_ADD
              140 STORE FAST
                                                 5 (zi)
 24
              143 LOAD GLOBAL
                                                2 (abs)
              146 LOAD FAST
                                                 5 (zi)
                                                 1
              149 CALL FUNCTION
              152 LOAD CONST
                                                6 (2.0)
              155 COMPARE OP
                                                4 (>)
              158 POP JUMP IF FALSE
                                              123
```

```
def calculate_z_numpy(q, maxiter, z):
    """use vector operations to update all zs and qs to create new output array"""
    output = np.resize(np.array(0,), q.shape)
    for iteration in range(maxiter):
        z = z*z + q
        done = np.greater(abs(z), 2.0)
        q = np.where(done, 0+0j, q)
        z = np.where(done, 0+0j, z)
        output = np.where(done, iteration, output)
    return output
```

numpy's strength is that it simplifies running the same operation on a vector (or matrix) of numbers rather than on individual items in a list one at a time.

If your problem normally involves using nested for loops to iterate over individual items in a list then consider whether numpy could do the same job for you in a simpler (and probably faster) fashion.

If the above code looks odd to you, read it as:

- z*z does a pairwise multiplication, think of it as z[0] = z[0] * z[0]; z[1] = z[1] * z[1]; ...; <math>z[n-1] = z[n-1] * z[n-1].
- z_result + q does a pairwise addition, just like the line above but adding the result
- $z = \dots$ assigns the new array back to z
- np.greater(condition, item_if_True, item_if_False) calculates the condition for each item in abs(z), for the nth value if the result is True it uses the item_if_true value (in this case 0+0j) else it uses the other value (in this case q[nth]) each item in q either resets to 0+0j or stays at the value it was before
- The same thing happens for z
- output's items are set to iteration if done[nth] == True else they stay at the value they were at previously.

```
>>>python numpy_vector.py 1000 1000
x and y have length: 500 500
Total elements: 250000
Main took 0:00:02.927419
Total sum of elements (for validation): 1148485
>>>python numpy_vector_2.py 1000 1000
x and y have length: 500 500
Total elements: 250000
STEP_SIZE 20000
Main took 0:00:02.488578
Total sum of elements (for validation): 1148485
```

```
def calculate_z_numpy(q, maxiter, z):
    """use vector operations to update all zs and qs
    output = np.resize(np.array(0,), q.shape)
    for iteration in range(maxiter):
        z = z*z + q
        done = np.greater(abs(z), 2.0)
        q = np.where(done, 0+0j, q)
        z = np.where(done, 0+0j, z)
        output = np.where(done, iteration, output)
    return output
```

```
output = np.resize(np.array(0,), q_full.shape)
\#STEP\_SIZE = len(q\_full) \# 54s for 250,000
#STEP_SIZE = 90000 # 52
#STEP_SIZE = 50000 # 45s
#STEP_SIZE = 45000 # 45s
STEP_SIZE = 20000 # 42s # roughly this looks optimal on Ma
#STEP SIZE = 10000 # 43s
#STEP_SIZE = 5000 # 45s
#STEP_SIZE = 1000 # 1min02
#STEP SIZE = 100 # 3mins
print "STEP_SIZE", STEP_SIZE
for step in range(0, len(q_full), STEP_SIZE):
    z = z_full[step:step+STEP_SIZE]
    q = q_full[step:step+STEP_SIZE]
    for iteration in range(maxiter):
        z = z*z + q
        done = np.greater(abs(z), 2.0)
        q = np.where(done, 0+0j, q)
        z = np.where(done, 0+0j, z)
        output[step:step+STEP SIZE] = np.where(done, itera
return output
```

def calculate_z_numpy(q_full, maxiter, z_full):

MULTIPROCESSING

The multiprocessing module lets us send work units out as new Python processes on our local machine (it won't send jobs over a network). For jobs that require little or no interprocess communication it is ideal.

We need to split our input lists into shorter work lists which can be sent to the new processes, we'll then need to combine the results back into a single output list.

We have to split our q and z lists into shorter chunks, we'll make one sub-list per CPU. On my MacBook I have two cores so we'll split the 250,000 items into two 125,000 item lists. If you only have one CPU you can hard-code nbr_chunks to e.g. 2 or 4 to see the effect.

```
# create a Pool which will create Python processes
p = multiprocessing.Pool()
start_time = datetime.datetime.now()
# send out the work chunks to the Pool
# po is a multiprocessing.pool.MapResult
po = p.map_async(calculate_z_serial_purepython, chunks)
# we get a list of lists back, one per chunk, so we have to
# flatten them back together
# po.get() will block until results are ready and then
# return a list of lists of results
results = po.get() # [[ints...], [ints...], []]
```

```
nagal:parallelpython_pure_python>python parallelpython_pure_python.py 1000 1000
Total elements: 250000
31250 8 31250
Starting pp with 8 local CPU workers
Submitting job with len(q) 31250, len(z) 31250
Job execution statistics:
 job count | % of all jobs | job time sum | time per job | job server
                    100.00
                                  14.2874 |
                                                1.785928 | local
Time elapsed since server creation 3.75450515747
0 active tasks, 8 cores
None
```

Main took 0:00:04.008474

Total sum of elements (for validation): 1148485

Parallel Python

import pp

```
# tuple of all parallel python servers to connect with
ppservers = () # use this machine
# I can't get autodiscover to work at home
#ppservers=("*",) # autodiscover on network
job_server = pp.Server(ppservers=ppservers)
# it'll autodiscover the nbr of cpus it can use if first arg not specified
print "Starting pp with", job_server.get_ncpus(), "local CPU workers"
output = []
jobs = []
for chunk in chunks:
    print "Submitting job with len(q) {}, len(z) {}".format(len(chunk[0]), len(chunk[2])
    job = job_server.submit(calculate_z_serial_purepython, (chunk,), (), ())
    jobs.append(job)
for job in jobs:
    output_job = job()
    output += output_job
# print statistics about the run
print job_server.print_stats()
```

Use the best algorithms and fastest tools

- Membership testing with sets and dictionaries is much faster, O(1), than searching sequences, O(n).
 When testing "a in b", b should be a set or dictionary instead of a list or tuple.
- String concatenation is best done with ''.join(seq) which is an O(n) process. In contrast, using the '+' or '+=' operators can result in an O(n**2) process because new strings may be built for each intermediate step. The CPython 2.4 interpreter mitigates this issue somewhat; however, ''.join(seq) remains the best practice.
- Many tools come in both list form and iterator form (range and xrange, map and itertools.imap, list comprehensions and generator expressions, dict.items and dict.iteritems). In general, the iterator forms are more memory friendly and more scalable. They are preferred whenever a real list is not required.
- Many core building blocks are coded in optimized C. Applications that take advantage of them can make substantial performance gains. The building blocks include all of the builtin datatypes (lists, tuples, sets, and dictionaries) and extension modules like array, itertools, and collections.deque.
- Likewise, the builtin functions run faster than hand-built equivalents. For example, map(operator.add, v1, v2) is faster than map(lambda x,y: x+y, v1, v2).
- Lists perform well as either fixed length arrays or variable length stacks. However, for queue applications using pop(0) or insert(0,v)), collections.deque() offers superior O(1) performance because it avoids the O(n) step of rebuilding a full list for each insertion or deletion.
- Custom sort ordering is best performed with Py2.4's key= option or with the traditional decorate-sort-undecorate technique. Both approaches call the key function just once per element. In contrast, sort's cmp= option is called many times per element during a sort. For example, sort(key=str.lower) is faster than sort(cmp=lambda a,b: cmp(a.lower(), b.lower())). See also TimeComplexity.

Take advantage of interpreter optimizations

- In functions, local variables are accessed more quickly than global variables, builtins, and attribute lookups. So, it is sometimes worth localizing variable access in inner-loops. For example, the code for random.shuffle() localizes access with the line, random=self.random. That saves the shuffling loop from having to repeatedly lookup self.random. Outside of loops, the gain is minimal and rarely worth it.
- The previous recommendation is a generalization of the rule to factor constant expressions out of loops. Likewise, constant folding needs to be done manually. Inside loops, write "x=3" instead of "x=1+2".
- Function call overhead is large compared to other instructions. Accordingly, it is sometimes worth inlining code inside time-critical loops.
- List comprehensions run a bit faster than equivalent for-loops (unless you're just going to throw away the result).
- Starting with Py2.3, the interpreter optimizes "while 1" to just a single jump. In contrast "while True"
 takes several more steps. While the latter is preferred for clarity, time-critical code should use the first
 form.
- Multiple assignment is slower than individual assignment. For example "x,y=a,b" is slower than "x=a; y=b". However, multiple assignment is faster for variable swaps. For example, "x,y=y,x" is faster than "t=x; x=y; y=t".
- Chained comparisons are faster than using the "and" operator. Write "x < y < z" instead of "x < y and y < z".
- A few fast approaches should be considered hacks and reserved for only the most demanding applications. For example, "not not x" is faster than "bool(x)".